

MAT126.R01: QUIZ 3

SOLUTIONS

Differentiate the following functions:

(a) $f(x) = \frac{2x}{\sqrt{x+1}}$

$$\left(\frac{2x}{\sqrt{x+1}}\right)' = \frac{(2x)'\sqrt{x+1} - 2x(\sqrt{x+1})'}{(\sqrt{x+1})^2} = \frac{2\sqrt{x+1} - 2x\frac{1}{2\sqrt{x+1}}}{x+1} = \frac{2(x+1) - x}{(x+1)\sqrt{x+1}} = \frac{x+2}{(x+1)^{3/2}}$$

using the chain rule to differentiate $\sqrt{x+1}$: $u = x+1$ and $(x+1)' = 1$,

$$(\sqrt{u})' = \frac{1}{2\sqrt{u}}.$$

(b) $g(t) = \cos(\ln(t+1))$

$$(\cos(\ln(t+1)))' = -\sin(\ln(t+1))\frac{1}{t+1} = -\frac{\sin(\ln(t+1))}{t+1}$$

using the chain rule with $u = \ln(t+1)$:

$$(\ln(t+1))' = \frac{1}{t+1} \text{ (this uses another chain rule with } u = t+1 \text{ and } (\ln u)' = \frac{1}{u} \text{ and } (\cos u)' = -\sin u.$$

(c) $w(z) = z^3 e^z$

$$(z^3 e^z)' = (z^3)'e^z + z^3(e^z)' = 3z^2 e^z + z^3 e^z = (3z^2 + z^3)e^z$$