

Problem 1 Simplify the following expression.

$$(x + y)^3 - (x - y)^3.$$

$$2y(3x^2 + y^2)$$

Problem 2 Find another form of the following expression (here $x > 1$ and $0 < h < 1$)

$$\frac{\sqrt{x+h} - \sqrt{x-h}}{h}.$$

$$2/(\sqrt{x+h} + \sqrt{x-h})$$

Problem 3 Find the region of the number line on which the inequality is valid.

$$3x^2 - 2x > 1.$$

$$x < -1/3 \text{ or } x > 1$$

Problem 4 A circle in the xy -plane has center on the x -axis and contains the points $(-2, 4)$ and $(5, 3)$. Find the x -coordinate of the center of the circle.

$$1$$

Problem 5 How many points of intersection are there between the parabola $y = x^2$ and the circle with center at $(1, 1)$ and radius $\sqrt{2}$?

$$\text{Two}$$

Problem 6 Reflect the parabola $y = x^2$ through the line $x = 1$. Next reflect the resulting parabola through the line $y = -1$. Find the region on which the final parabola is increasing.

$$x \leq 2$$

Problem 7 Consider the following one-to-one function $f(x)$ on the given interval.

$$f(x) = \frac{x}{1+x^2}, \quad 1 \leq x < \infty$$

Find the domain of the inverse function $f^{-1}(x)$.

$$(0, 1/2]$$

Problem 8 A sector of a circle subtends an angle of $\pi/3$ radians and has an area of 6π square cm. Find the arc length of the portion of the circumference in this sector.

$$2\pi \text{ cm}$$

Problem 9 Compute $\tan(4\pi/3)$.

$$\sqrt{3}$$

Problem 10 Find an equivalent form of $\sin(3\theta)$.

$$-4\sin^3(\theta) + 3\sin(\theta)$$