

$$(5) \quad 0 \leq \rho \leq 1, \quad 0 \leq \theta \leq 2\pi, \quad 0 \leq \phi \leq \pi/4$$

$$(6) \quad a). \quad \gamma'(t) = \langle 3 \cos 3t, -3 \sin 3t, 3 t^{1/2} \rangle$$

Parametric equations for the tangent line
at $t = \pi$:

$$x = -3t$$

$$y = -1$$

$$z = 2\pi^{3/2} + t \cdot 3\pi^{1/2}$$

$$\left(\begin{array}{l} \gamma(\pi) = \langle 0, -1, 2\pi^{3/2} \rangle \\ \gamma'(\pi) = \langle -3, 0, 3\pi^{1/2} \rangle \end{array} \right)$$

$$(8) \quad \gamma(t) = \left\langle \frac{2}{1+t^2} - 1, \frac{2t}{1+t^2} \right\rangle = \left\langle \frac{1-t^2}{1+t^2}, \frac{2t}{1+t^2} \right\rangle$$

Arc length

Parametrization: * $(1, 0)$ corresponds to $t = 0$

$$s = s(t) = \int_0^t \|\gamma'(u)\| \, du = \int_0^t \frac{2}{1+u^2} \, du = 2 \tan^{-1} t \quad (= 2 \arctan t)$$

$$s = 2 \tan^{-1} t \Rightarrow \tan\left(\frac{s}{2}\right) = t = t(s)$$

$$\therefore \gamma(t(s)) = \left\langle \frac{2}{1 + \tan^2\left(\frac{s}{2}\right)} - 1, \frac{2 \tan\left(\frac{s}{2}\right)}{1 + \tan^2\left(\frac{s}{2}\right)} \right\rangle$$

$$= \left\langle \frac{2}{\sec^2\left(\frac{s}{2}\right)} - 1, \frac{2 \tan\left(\frac{s}{2}\right)}{\sec^2\left(\frac{s}{2}\right)} \right\rangle = \langle \cos s, \sin s \rangle$$

the \uparrow unit circle!