

**MAT 615: Complex Curves and Surfaces
Spring 2009**

Problem Set 1

Due on Tuesday, 2/10, at 12:40pm

Please write up concise solutions to 3 of the following problems; half a page for each should suffice.

Problem 1 (5 pts)

Let $C \subset \mathbb{P}^n$, with $n \geq 3$, be a any curve. Show that there exists a point $p \in \mathbb{P}^n$ which is not contained on any line in \mathbb{P}^n meeting C in at least 3 points. (this is related to p215 bottom)

Problem 2 (5 pts)

How does the second statement of Abel's theorem on p227 imply the first?

Problem 3 (5 pts)

The period matrix Ω on p228 is the matrix of a certain natural homomorphism with respect to certain bases. What are these?

Problem 4 (5 pts)

Show that $\mathbb{P}^{1(d)} = \mathbb{P}^d$ (see p236).